

B.Sc. ELECTRONICS
First Semester
MATHEMATICS-I
(BSE - 104)

Duration: 3Hrs.

Full Marks: 70

Part-A (Objective) =20
Part-B (Descriptive) =50

(PART-B: Descriptive)

Duration: 2 hrs. 40 mins.

Marks: 50

I. Answer any five of the following questions:

1. Find the modulus and argument of the complex numbers, $\frac{1+i}{1-i}$ and $\frac{2+3i}{i}$. (6+4=10)

Express $\frac{(\cos \theta + \sin \theta)^8}{(\sin \theta + \cos \theta)^4}$ in the form $x+iy$.

2. (i) Find the middle term of $(x+2)^7$ and $\left(2x+\frac{1}{x}\right)^{14}$. (5+5=10)

(ii) Show that

$$\left(1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots\right) - \left(x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots\right) = 1$$

3. (i) Solve the equation $2x^3 + 3x^2 - 32x - 48 = 0$, given that the sum of any two roots are zero.

(ii) Solve the equation $2x^3 - 3x^2 - 6x + 8 = 0$, given that the roots are in A. P. (5+5=10)

4. Write any two properties of (i) matrix multiplication and (ii) transpose of matrix.

Find AB and BA , where, $A = \begin{pmatrix} 2 & 1 & 3 \\ -1 & 4 & -6 \\ 7 & 1 & 2 \end{pmatrix}$ and $B = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 4 & 5 \\ 0 & 2 & 1 \end{pmatrix}$. (4+6=10)

5. Solve the following system of equations $x+y+z=6$, $x+2z=7$, $3x+y+z=12$ by using

(i) matrix method (ii) Cramer's rule. (5+5=10)

6. Define inverse of a square matrix. Find A^{-1} , where $A = \begin{pmatrix} 1 & 2 & 3 \\ 1 & 0 & 1 \\ -1 & 2 & 3 \end{pmatrix}$. Prove $AB=BA=I$,

where $B = \frac{adjA}{|A|}$. (2+6+2=10)

7. Separate the following into real and imaginary part: (2×5=10)

(i) $\sin(x+iy)$ (ii) $\cos(x+iy)$ (iii) $\tan(x+iy)$

(iv) $\cot(x+iy)$ (v) $\sec(x+iy)$ (vi) $\operatorname{cosec}(x+iy)$

8. Express, (i) $\sin^7 \theta$ as a sum of sines of multiples of θ . (5+5=10)

(ii) $\cos^8 \theta$ as a sum of cosines of multiples of θ .

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Marks – 20

(PART A - Objective Type)

I. Choose the correct answer:

1×20=20

- Sum of the roots of the equation $x^5 + 3x^4 + 4x^3 + 12 = 0$ is
(i) 3 (ii) -3 (iii) 1 (iv) -1
- Sum of the products of the roots taken two at a time of the $x^5 + 2x^4 + 2x^3 + x = 0$ is
(i) 2 (ii) -2 (iii) 1 (iv) -1
- The cofactor of -2 in the matrix $\begin{pmatrix} 4 & -2 \\ 1 & 3 \end{pmatrix}$ is
(i) 3 (ii) -4 (iii) -1 (iv) 1
- The rank of the matrix $\begin{pmatrix} 3 & -7 \\ -3 & 7 \end{pmatrix}$ is
(i) 0 (ii) 1 (iii) 2 (iv) None of these
- If A is a 3×3 matrix and $|A| = 3$, then $|3A| =$
(i) 3 (ii) 9 (iii) 27 (iv) 81
- If $\begin{pmatrix} 1 & 2 & 0 \\ 8 & x & -1 \\ 2 & 4 & 5 \end{pmatrix} = \begin{pmatrix} 1 & 2 & 0 \\ 8 & 9 & -1 \\ 2 & 4 & 5 \end{pmatrix}$, then the value of x is
(i) 0 (ii) 2 (iii) 9 (iv) 5
- If $A = \begin{pmatrix} 1 & 0 & 0 \\ 2 & -3 & 0 \\ 4 & 5 & 6 \end{pmatrix}$, then $|A|$ is
(i) 1 (ii) 4 (iii) -1 (iv) -18
- If $z = a + ib$ then $z + 2\bar{z}$ is
(i) 4a (ii) 2a (iii) ib (iv) 2ib

9. The real part of $\frac{2-3i}{2+i}$ is

- (i) $\frac{1}{5}$ (ii) $\frac{7}{5}$ (iii) $-\frac{1}{5}$ (iv) $-\frac{2}{5}$

10. $(\cos\theta + i\sin\theta)^n =$

- (i) $\cos n\theta + i\sin n\theta$ (ii) $\cos n\theta - i\sin n\theta$
(iii) $e^{in\theta}$ (iv) None of these

11. $\sin\theta =$

- (i) $\frac{e^{i\theta} + e^{-i\theta}}{2}$ (ii) $\frac{e^{i\theta} - e^{-i\theta}}{2}$ (iii) $e^{i\theta} - e^{-i\theta}$ (iv) $e^{i\theta} + e^{-i\theta}$

12. The value of $\cosh 0$ is

- (i) 1 (ii) $\frac{1}{2}$ (iii) 0 (iv) $\frac{1}{\sqrt{2}}$

13. Which of the following is true?

- (i) $\sin ix = \sinh x$ (ii) $\cos ix = \cosh x$
(iii) $\tan ix = \tanh x$ (iv) $\cot ix = \coth x$

14. Which of the following is not true?

- (i) $e^\theta + e^{-\theta} = 2\cosh\theta$ (ii) $e^\theta - e^{-\theta} = 2\sinh\theta$
(iii) $e^{i\theta} = \cos\theta + i\sin\theta$ (iv) $e^\theta - e^{-\theta} = 2i\sinh\theta$

15. Modulus of $-\sqrt{3} - i$ is

- (i) 1 (ii) 2 (iii) 3 (iv) 4

16. If α, β, γ are the roots of the equation $x^3 + px^2 + qx + r = 0$ the $\alpha\beta\gamma = ?$

- (i) p (ii) q (iii) r (iv) $-r$

17. The middle term in the expansion of $(a+x)^n$, when n is even is

- (i) $C_{\frac{n}{2}}^n a^{\frac{n}{2}} x^{\frac{n}{2}}$ (ii) $C_{\frac{n}{2}}^n a^n x^{\frac{n}{2}}$ (iii) $C_{\frac{n}{2}}^n a^{\frac{n}{2}} x^n$ (iv) $C_{\frac{n}{2}}^n a^n x^n$

18. The general term T_{r+1} in the expansion of $(a+x)^n$ is

- (i) $C_r^n a^{n-r} x^r$ (ii) $C_r^n a^r x^{n-r}$ (iii) $C_{\frac{n}{2}}^n a^{\frac{n}{2}} x^n$ (iv) $C_{\frac{n}{2}}^n a^n x^n$

19. Which of the following is correct?

- (i) $e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots \infty$ (ii) $e^x = 1 + x + \frac{x^2}{2} + \frac{x^3}{3} + \dots \infty$
(iii) $e^x = 1 + x + \frac{x^2}{2} + \frac{x^4}{4} + \dots \infty$ (iv) $e^x = 1 + x + \frac{x^3}{3} + \frac{x^5}{5} + \dots \infty$

20. If A and B are two square matrix of same order and $AB=BA=I$, then which of the following is correct,

- (i) $B = \frac{\text{adj}A}{|A|}$ (ii) $B = \text{adj}A$ (iii) $B = \frac{\text{adj}A}{|B|}$ (iv) $A = \frac{\text{adj}B}{|A|}$
