

**B.SC. CHEMISTRY
THIRD SEMESTER
VECTOR ANALYSIS
BSM – 732**

**SET
A**

[USE OMR FOR OBJECTIVE PART]

Duration: 1.30 hrs.

Full Marks: 35

(PART-A: Objective)

Time: 15 min.

Marks: 10

Choose the correct answer from the following:

1X10=10

- The value of $-\hat{i}(\hat{k} \times \hat{j})$ is
 - 1
 - 1
 - 0
 - None of these
- If two vectors \vec{a} and \vec{b} are parallel then $\vec{a} \times \vec{b}$ is
 - 0
 - A non-zero vector
 - any vector
 - None of these
- The unit tangent vector at any point of the curve $x = 3 \cos \theta, y = 3 \sin \theta, z = 4\theta$ is:
 - 3
 - 4
 - 5
 - 6
- If $\theta = 3x^2y - y^3z^2$, then gradient at the point $(1, -2, -1)$ is
 - $-12\hat{i} + 9\hat{j} + 16\hat{k}$
 - $-12\hat{i} - 9\hat{j} + 16\hat{k}$
 - $-12\hat{i} - 9\hat{j} - 16\hat{k}$
 - None of these
- If $\vec{F} = (x^2 - y^2 + x)\hat{i} - (2xy + y)\hat{j}$, the $\text{curl}(\vec{F})$ is
 - 0
 - $4y\hat{k}$
 - $\hat{i} + \hat{j} + \hat{k}$
 - None of these
- The unit vector in the direction of vector $\vec{a} = 2\hat{i} + 3\hat{j} + \hat{k}$ is
 - $\frac{1}{\sqrt{14}}(2\hat{i} + 3\hat{j} + \hat{k})$
 - $-2\hat{i} - 3\hat{j} + \hat{k}$
 - $\frac{1}{\sqrt{14}}(2\hat{i} + 3\hat{j} + \hat{k})$
 - None of these
- If \vec{a} and \vec{b} are two collinear vectors, then which of the following are incorrect?
 - $\vec{b} = \lambda\vec{a}$, for some λ
 - $\vec{b} = \pm\vec{a}$
 - Both the vectors \vec{a} and \vec{b} have same direction, but different magnitudes.
 - None of these

(PART-B : Descriptive)

Time : 1 hr. 15 min.

Marks : 25

[Answer question no.1 & any two (2) from the rest]

1. Find the vector triple product for the vectors 5
 $\vec{a} = \hat{i} + \hat{j} - \hat{k}$, $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ and $\vec{c} = \hat{i} - \hat{j} - \hat{k}$
2. a. Let $\vec{a} = 3\hat{i} + \hat{j} + 2\hat{k}$ and $\vec{b} = 2\hat{i} - 2\hat{j} + 4\hat{k}$. Find: 2×3+4
=10
(i) $\vec{a} \times \vec{b}$
(ii) $|\vec{a} \times \vec{b}|$
(iii) Unit vector perpendicular to \vec{a} and \vec{b} .
- b. Find the angle between the vector $\vec{a} = 2\hat{i} + 3\hat{j} - \hat{k}$ and $\vec{b} = 3\hat{i} + \hat{j} + 2\hat{k}$.
3. a. Find the divergence and curl of 6+4=10
 $\vec{F} = (xyz)\hat{i} + (3x^2y)\hat{j} + (xz^2 - y^2z)\hat{k}$
at $(2, -1, 1)$.
- b. Find the rate of change of $\phi = xyz$ in the direction normal to the surface $x^2y + y^2x + yz^2$ at the point $(1, 1, 1)$.
4. a. If $u = x + y + z$, $v = x^2 + y^2 + z^2$ and $w = xz + yz + xy$. Prove 6+4=10
that $\text{grad } u$, $\text{grad } v$ and $\text{grad } w$ are coplanar vector.
- b. If $\vec{a} \times \vec{b} = \vec{c} \times \vec{a}$ and $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$ then show that $-\vec{a} - \vec{d}$ is parallel to $\vec{b} - \vec{c}$.

5. a. Find the directional derivatives of $x^2y^2z^2$ at the point $(1, 1, -1)$ in the direction of the curve $x = e^t, y = \sin 2t + 1$ and $z = 1 - \cos t$ at $t = 0$.

6+4=10

b. If \vec{a}, \vec{b} and \vec{c} are the position vectors of the vertices A, B, C respectively of a triangle ΔABC then prove that -

$$(\vec{a} - \vec{c}) + (\vec{c} - \vec{b}) + (\vec{b} - \vec{a}) = 0$$

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